



# **Will GEO Work? – An Economist's View**

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# Background

- **GEO**
- **GEOSS**
  - G8 initiative to bring observing systems in line to address concerns of society
  - 9 Benefit Areas which a perfect GEO system should cover (*Disaster, Health, Energy, Climate, Water, Weather, Ecosystems, Agriculture and Biodiversity*)
- **GEO-BENE**
  - Assessment of economic, social and environmental benefits of improved information provided in the context of GEOSS in the short and long-term

# Modeling

- Aggregated macroeconomic model of a society under the threat of extreme events (catastrophes)
- **GEOSS:**
  - Preventive measures to increase society's welfare
- **Global Partnership:**
  - “Investment Game” in multi-society world

# Model

Stylized neoclassical model of the development of an economy affected<sup>[1]</sup> by random natural hazards

**Capital stock dynamics:**  $K_{i+1} = ((1 - \delta)K_i + I_{i+1}) \cdot D_{i+1}, \quad i = 0, 1, \dots, \infty$

Here  $K_i$  – capital,  $D_i$  – extreme event (random variable),  
 $I_i$  – investment,  $C_i$  – consumption

Production output  $Y_{i+1} = \alpha K_i$

Step 1:  $Y_1 = I_1 + C_1 + Z$

investment in the development  
of prevention measures

Step  $i > 1$ :  $Y_{i+1} = I_{i+1} + C_{i+1}$

**Social planner** chooses consumption level in order to **maximize** the economy's utility, expected value of the **social welfare**

$$W(z) = \max_{C_i} E \left( \sum_{i=0}^{\infty} (1 + \rho)^{-i} \ln C_{i+1} \right)$$

[1] Z. Chladna, E. Moltchanova, and M. Obersteiner, "Prevention of Surprise", in: S. Albeverio, V. Jentsch, H. Kantz (Eds.), Extreme Events in Nature and Society, Springer, vol. 352, pp. 295–318, 2006.

# Model

Capital stock dynamics:

$$K_{i+1} = ((1 - \delta)K_i + I_{i+1}) \cdot D_{i+1}, \quad i = 0, 1, \dots, \infty$$

Extreme event  $D_i$  occurs with probability  $q_i$  causing the loss of fraction  $d$  of the capital stock:

$$D_i = \begin{cases} 1 - d, & \text{with probability } q_i \\ 1, & \text{with probability } 1 - q_i \end{cases}$$

Probability  $q_i$  endogenously depends on the preventive measures  $z$

$$q_i = \frac{q_0}{1 + \kappa z}, \quad i = 1, 2, \dots$$

Here  $q_0$  is the probability of disasters without any preventive measures, and  $\kappa$  is a given positive coefficient characterizing the efficiency of investment.

# Optimal Welfare

**Proposition<sup>[2]</sup>.** *For every  $z \in [0, \alpha K_0)$ , the **optimal social welfare**  $W(z)$  has the following form*

$$W(z) = \log(1 - s_0) + \frac{1}{\rho} \log((1 - \delta)K_0 + s_0(\alpha K_0 - z)) \\ + \log(\alpha K_0 - z) + \frac{1}{\rho} \log \rho + \frac{1+\rho}{\rho^2} \log \rho \left( \frac{\alpha+1-\delta}{1+\rho} \right)$$

where

$$s_0 = \begin{cases} \frac{\alpha K_0 - z - \rho(1-\delta)K_0}{(\alpha K_0 - z)(1+\rho)} & \text{if } z < (\alpha + \rho\delta - \rho)K_0, \\ 0 & \text{otherwise} \end{cases}$$

[2] A. Kryazhimskiy, M. Obersteiner, and A. Smirnov, "Infinite-horizon dynamic programming and application to management of economies effected by random hazards", Appl. Math. Comput., 205, pp. 609–620, (doi:10.1016/j.amc.2008.05.042), 2008.

# Optimal Preventive Measures

How big should be the investment  $z$  into preventive measures to provide the best value for the social welfare?

**Optimal investment problem:**

Maximize  $W(z)$  over all  $z \in [0, \alpha K_0)$ .

**Proposition.** *Optimal investment problem has the unique solution  $z^*$ .  
If*

$$\alpha K_0 |q_0 \log(1-d)| \leq \frac{\rho(1+\rho)}{1+\alpha-\delta},$$

*then  $z^*=0$ , otherwise  $z^*$  is positive (for exact formula see ([2])).*

[2] A. Kryazhimskiy, M. Obersteiner, and A. Smirnov, "Infinite-horizon dynamic programming and application to management of economies effected by random hazards", Appl. Math. Comput., 205, pp. 609–620, (doi:10.1016/j.amc.2008.05.042), 2008.



# Optimal Preventive Measures

## Qualitative conclusion

- Economy refrains from investing in the prevention measures if its ability to cope with natural hazards ( $\kappa K_0$ ) is low, or the measure of danger, caused by natural hazards ( $|q_0 \log(1-d)|$ ) is not high enough.



# Investment Game

- Two independent economies both under the threat of natural disasters
- Each of the economies can make an investment ( $z^1$ ,  $z^2$ ) in common prevention measures aimed at mitigating the impact of natural hazards on both economies
- Each economy is subject the same dynamics as on the previous slides but with its own set of parameters (indicating by corresponding indexes).

# Investment Game

Effect of joint investments is achieved by the modification of the rule how probability of the occurrence of natural hazards changes after the implementation of prevention measures

$$q_i = \frac{q_0}{1 + \kappa^1 z^1 + \kappa^2 z^2}, \quad i = 1, 2, \dots$$

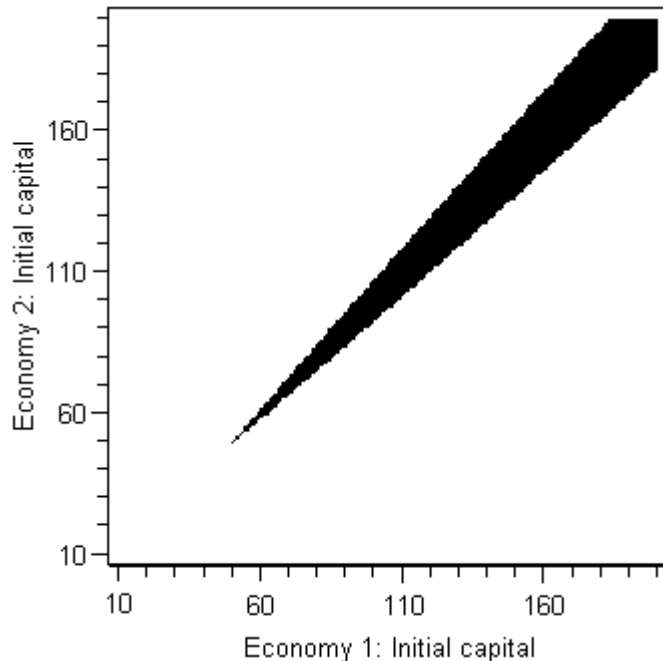
Each economy is maximizing its own welfare

Maximize  $W_1(z^1, z^2)$  over all  $z^1 \in [0, \alpha^1 K_0^1]$ .

Maximize  $W_2(z^1, z^2)$  over all  $z^2 \in [0, \alpha^2 K_0^2]$ .

**Proposition.** *Non-zero-sum game of preventive investments always has a unique Nash equilibrium solution  $(z^{1*}, z^{2*})$ .*

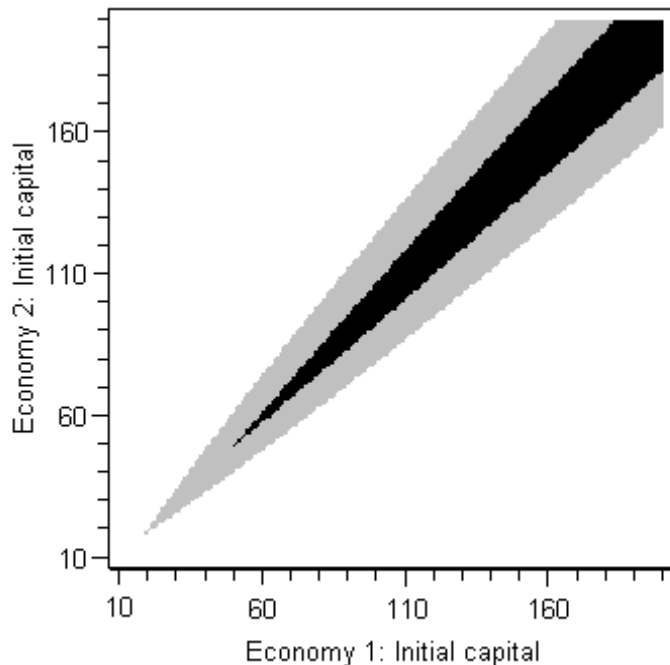
# Investment Game



It can be shown that in the context of **perfect knowledge** about model's parameters the case when both economies invest ( $z^{i*} > 0$ ) into preventive measures (we call this **cooperative behavior**) happens **only among similar economies**.

Figure shows the example how narrow is the **"cooperation zone"** (economies' initial capitals must belong to the black area to reveal the cooperative behavior).

# Investment Game: **Role on Uncertainties**



Taking into account **uncertainties** naturally existing in the model (parameters like probability of natural disasters,  $q_0$  and their impact on capital stock,  $d$ ) we found that for some of previously non-cooperative economies there will appear **additional cooperative solutions**.

Figure shows that **10% uncertainty** in the probability ( $q_0$ ) of occurring of natural disaster leads to the increasing of **“cooperation zone” more than twice**. Grey area on the figure describes the economies where **cooperation becomes an option**.

# Conclusions

- Emergence of a joint GEOSS infrastructure as a Global Partnership is unlikely to materialize basing only on economical interests:
  - “Rich” always pays in its own interest
  - Involving “Poor” only under special cases
  - Free-rider problem to establish global infrastructure
- Uncertainty in risk valuing provides an incentive for cooperation
- Arising non-uniqueness of equilibrium solutions leads to necessity of additional negotiations between countries to set appropriate investments level